Examination Number:			
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Sign the Honor Pledge Below	PID # Write Your Section Number here:		
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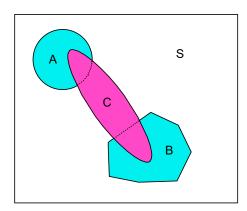
University of North Carolina Economics 400: Economic Statistics & Econometrics First Midterm Examination

Prof. B. Turchi

General Instructions: Answer all 9 questions on this examination, writing your answers on the exam paper itself. Use the back of the pages for any extra work, if necessary. Sign the Honor Pledge above. Express all answers to a precision of at least 3 decimal points. Show your work to be eligible for partial credit. Be sure to note that tables and formulas are on the last 2 pages of the exam.

Part I: Each question in this part (6 questions in all) is worth 5 points.

1. (5 points) Suppose we have three events A, B, and C in a sample space, S as shown in the Venn diagram below. Write the expression for the probability of event C in terms of the sample space and events A and B. P(C) =

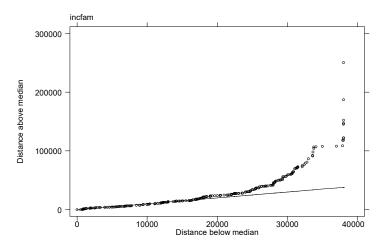


2. (5 points) Suppose we have events A_1 , A_2 , A_3 , that are exhaustive and mutually exclusive, then for any event, B, complete the expression, and draw a Venn diagram illustrating this situation.

$$P(B) = \underline{\hspace{1cm}}.$$

Venn diagram		

3. (5 points) Often we collect data and want to get an idea of the shape of the empirical distribution of those data. Below we have a **symmetry plot** for family income data drawn from a sample survey of households.



Describe the shape of this sample of family income data. Is it symmetrical? skewed (if so, in which direction)? Sketch a histogram of these data in the box to illustrate your answer



4. (5 points) Which of the following Stata commands prints out on the log the highest and lowest values of the variable *score* in a data set containing many variables? (Circle correct answer)

```
list score in 30/80
list if (score <30 | score >80)
list if (score >30 | score >80)
list if (score <30 & score > 80)
```

- 5. (5 points) Write below the Stata command that would give you the descriptive statistics for the variable *score*, including the mean, the median, the quartiles and the extreme values.
- 6. (5 points) In how many states does annual beer consumption exceed 22.9 gallons per capita?

```
. stem galperca
Stem-and-leaf plot for galperca (State Beer Consumption- Gal. Per Capita)
galperca rounded to nearest multiple of .1
plot in units of .1

1** | 30
1** |
1** | 73,75,79
1** | 88,93,93,95,98

2** | 00,01,01,03,05,07,07,08,10,10,13,13,16,18
2** | 21,22,25,29,29,30,33,35,35
2** | 40,41,44,44,46,49,49,52,56
2** | 64,67,69,70,70,70,78
2** | 86
3** | 13
3** |
3** | 44
```

Part II: The next 3 questions have multiple parts and are worth 70 points in total; be sure to answer all parts.

7. (25 points total) Despite the national furor over the arrival of the West Nile virus, the number of severe reported cases (projected to be 3,619 in 2002) is relatively small and the number of deaths resulting from those cases is also projected to be small (192 deaths). The West Nile virus is transmitted to humans through the bite of an infected mosquito. At present only about 0.5 percent of all mosquitos are infected with West Nile virus. Use the following information to answer the questions below:

Probability of being bitten by a mosquito: 0.35 Probability of catching the disease if bitten: 0.005 Probability of having a severe case if infected: 0.002 Probability of dying if have a severe case: 0.09

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B = bitten by a mosquito

C =catch the disease

S = have a severe case

D = die from West Nile fever

- a) (3 points) Write symbolically and numerically the probability of being bitten: $\underline{P(\underline{})} = \underline{\underline{}}$
- b) (3 points) Write symbolically and numerically the probability of catching the disease if bitten: P() =
- c) (3 points) Write symbolically and numerically the probability of having a severe case if infected: P(____) =__
- d) (3 points) Write symbolically and numerically the probability of dying if have a severe case: $\underline{P()} = \underline{ }$
- e) (13 points) compute the probability [P(D)] that a randomly selected person will die from the West Nile virus in 2002. Show the requested probability statement in symbolic terms and then use the information above to compute the probability of dying. Be sure to show your work.

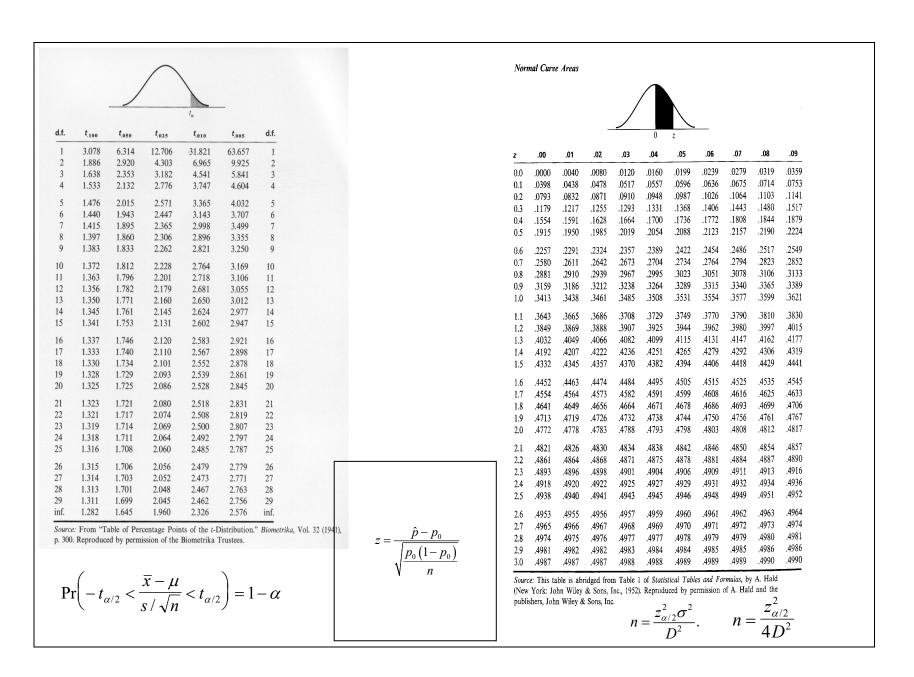
8.	standa Placer studer these	(25 points total) School districts pride themselves on the performance of their students on standardized tests of achievement and ability. A good example is the Advanced Placement Test for calculus. Suppose that the Wake County School district has 540 students enrolled in AP calculus. Based on prior years' experience we can expect 151 of these students to score a 4 or better on the AP calculus test. Suppose that we randomly sample 26 different students from the current group.		
	a)	(4 points) What is the expected number of students in this sample who receive a 4 or better on the AP test?		
	b)	(4 points) What is the variance of this sample?		
	c)	(9 points) What is the probability that between 6 and 13 students inclusive score a 4 or better on the exam?		
	d)	(4 points) What is the theoretically most appropriate distribution to use in calculating the answer to part c)? Why?		
	e)	(4 points) What distribution did you use to calculate the answer to part c)? Why?		

9.	(20 points total) A couple of years ago, my children bought me a DVD player for Christmas. It had a one-year warranty and failed completely 376 days after purchase. In buying a new one, I was faced with the problem of buying an extended warranty that would extend warranty coverage through the 3d year of ownership (i.e., the extended warranty would expire on the 4th anniversary of purchase). The machine cost me \$250 new and would (we will assume) cost me the same to replace if it should fail. Finally, the salesman at BestBuy (an economics student at UNC) told me that he had seen company data suggesting that the mean time before failure of these machines is 3.2 years.			
	a)	(2 points) What is the probability that the machine will fail in <i>less than</i> zero years after purchase?		
	b)	(6 points) What is the probability that the machine will fail between 1 and 4 years?		
	c)	(6 points) What is the <i>maximum</i> that I should pay for the extended warranty?		
	d)	(6 points) If BestBuy has to replace my machine during warranty, it will cost them \$150 to do so. What is the <i>minimum</i> they will be willing to charge for the extended warranty?		

10.	(30 points) The owner of a local Mercedes Benz dealership is trying to sell the dealership to a buyer who wants to know the profit he can make if he buys the dealership. The dealer claims that he sells 1,200 cars per year at an average profit of \$4,400 per car. The number of cars sold each year is easily established to be, in fact, 1,200; however, the profit per car is more difficult to establish and requires the buyer to hire an accountant to compute the actual profits on cars from a random sample of last year's sales. The buyer needs to be confident at the 95 percent level that the profit per car is at least \$3,900 per car.
is ma	How many cars need to be sampled if we do not know whether the underlying distribution normal, but we do know that the underlying standard deviation, σ , is \$800 and we want a argin of error between the sample mean and population mean of no more than \$200. What stribution will you assume for the sampling distribution of the sample mean? Why?

b) Assume that a random sample of the size you just computed in part a) is drawn and the sample mean profit is \$4,110. Assuming the same population standard deviation as above, can we be 95 percent sure that the *minimum* profit is greater than or equal to \$3,900? Show your work and sketch a diagram illustrating your calculation.

c) Is the dealer's claimed profit within the 95 percent confidence interval suggested by the above sample? (Again, sketch a diagram illustrating your answer)



Binomial Coefficients

11 1 11 55 165 330 462 462 12 1 12 66 220 405 792 924 13 1 13 78 286 715 1287 1716 1 14 1 14 91 364 1001 2002 3003 3 15 1 15 105 455 1365 3003 5005 6 16 1 16 120 560 1820 4368 8008 11			$\binom{n}{10}$
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19 1 19 171 969 3876 11628 27132 50	0388 7558	92378	92378
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If necessary, use the identity $\binom{n}{k} = \binom{n}{n-k}$.

$$f(\widetilde{x}) = \frac{1}{\sigma\sqrt{2\pi}}e^{-(x-\mu)^2/2\sigma^2} - \infty < x < \infty$$

$$\sigma^{2} = \frac{\sum_{i=1}^{N} (x_{i} - \mu)^{2}}{N}$$

$$p(x) = \frac{C_{x}^{r} C_{n-x}^{N-r}}{C_{n}^{N}} = \frac{\binom{r}{x} \binom{N-r}{n-x}}{\binom{N}{n}}$$

$$\text{Mean: } \mu = n \left(\frac{r}{N}\right)$$

$$\text{Variance: } \sigma^{2} = n \left(\frac{r}{N}\right) \left(\frac{N-r}{N}\right) \left(\frac{N-n}{N-1}\right)$$

$$\text{Standard deviation: } \sigma = \sqrt{\sigma^{2}}$$

$$f(x) = \begin{cases} \frac{1}{(b-a)}, & a \le x \le b \\ 0, & \text{otherwise} \end{cases}$$

$$\mu = \frac{1}{2}(b+a) \text{ and } \sigma = \frac{(b-a)}{\sqrt{12}}$$

$$f(x) = \begin{cases} \lambda e^{-\lambda x}, & \lambda > 0, x \ge 0 \\ 0, & \text{otherwise} \end{cases}$$

$$\mu = \frac{1}{\lambda} \text{ and } \sigma = \frac{1}{\lambda}$$

$$P(x \ge a) = e^{-\lambda a}, a \ge 0 \text{ and } \lambda > 0$$

$$P(A_i|B) = \frac{P(B|A_i)P(A_i)}{\sum_{\text{all } k} P(B|A_k)P(A_k)}$$

$$P(x) = \begin{cases} \frac{e^{-\lambda t} (\lambda t)^{x}}{x!}, & \text{for } x = 0, 1, 2, , \infty, \quad \lambda > 0, \\ \frac{x!}{0}, & \text{otherwise.} \end{cases}$$

 λ = the mean number of events in a given segment of time (t = 1)

t = the length of a particular subsegment $(t \le 1)$

 $E[x] = \mu_x = \lambda t$ = the expected number of events in one subsegment length t